

# How Do We Learn to Use Learning in Manufacturing Systems?

**Kira Barton**

Robotics Department  
Department of Mechanical Engineering  
University of Michigan



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Zahra Afkhami  
Lucid Motors



Berk Altin  
NVIDIA



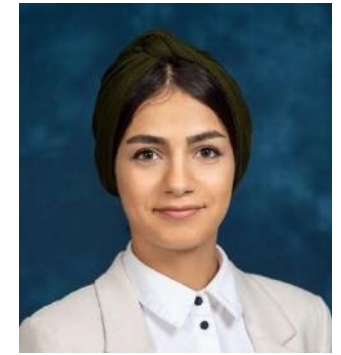
Christopher Pannier  
UM – Dearborn



Efe Balta  
ETH



Isaac Spiegel  
Terran Orbital



Nazanin Farjam  
UM



Mamadou Diagne  
UCSD



Patrick Sammons  
Quantitative  
Strategies



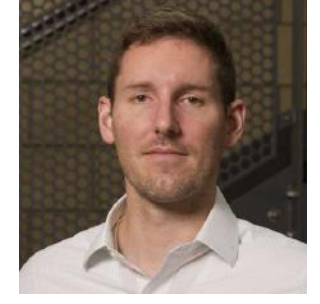
Leontine Aarnoudse  
TU/e



Tom Oomen  
TU/e



Ferdous Alam  
OSU



David Hoelzle  
OSU



# Outline

## **Basic Overview: Learning in Manufacturing**

### Learning Case Study:

- A. Challenges in additive manufacturing modeling and control
- B. Learning applied to an additive manufacturing example

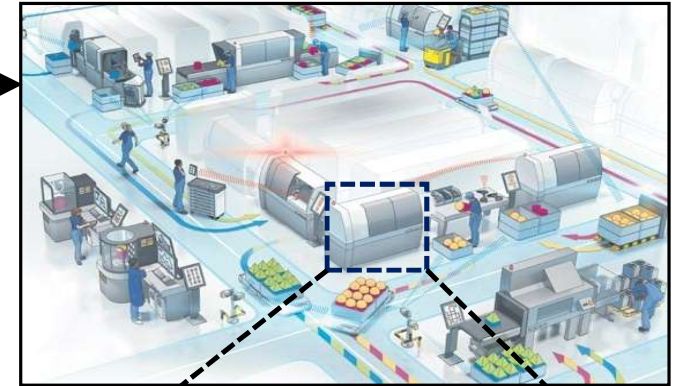
## Open Opportunities for Learning + Control to Advance Manufacturing

## Learning in Manufacturing

- Ability to derive a new understanding of a system using *information* from the *system+*
- Applying the new knowledge towards an updated 'model/reference signal/controller' to enhance system performance

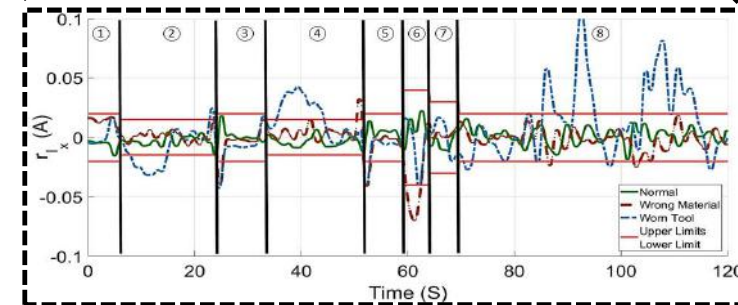
### System+

- Resources
- Operators
- SMEs
- Supply chain
- Environment
- Other systems

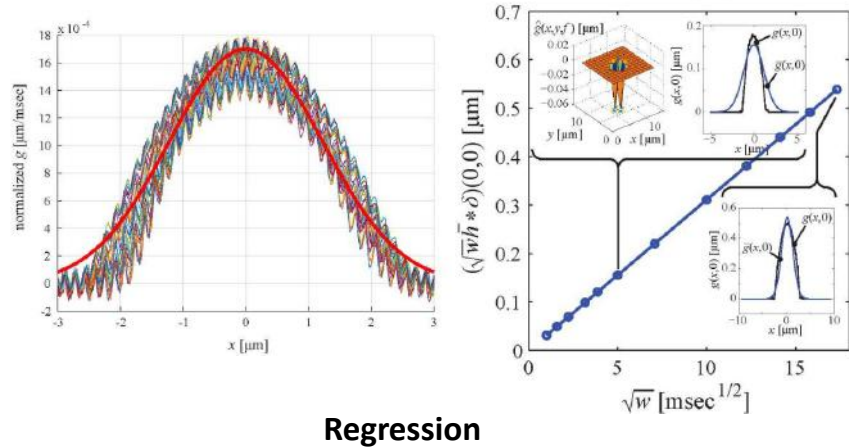


### Information

- Sensor data
- SME knowledge
- Physics-based models
- Historical data

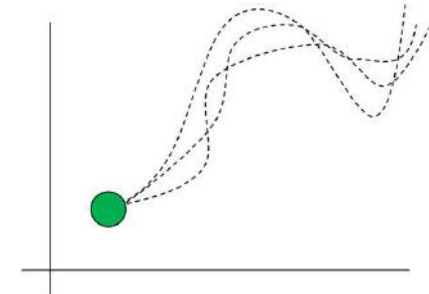


## Common methods of learning applied in manufacturing systems



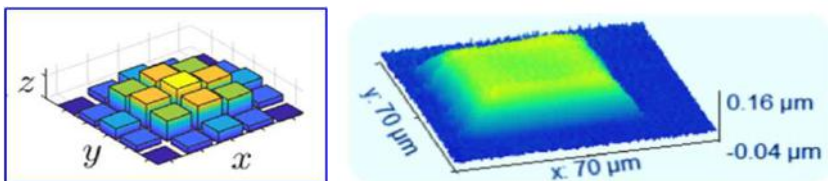
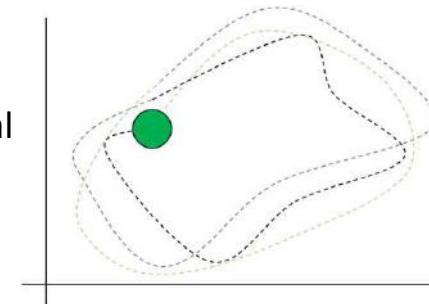
### Iterative Learning Control (ILC)

**Batch process:** Initial condition reset



### Repetitive Control (RC)

**Continuously-operated process:** Initial condition is given by terminal condition at previous cycle



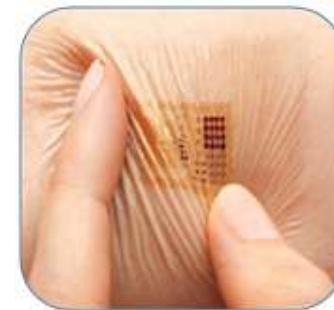
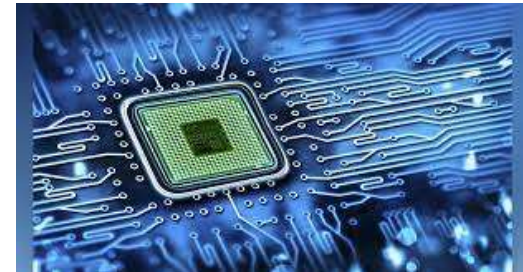
Convolutional Recurrent Neural Nets

Data-driven modeling

Repetitive and Adaptive Control Strategies

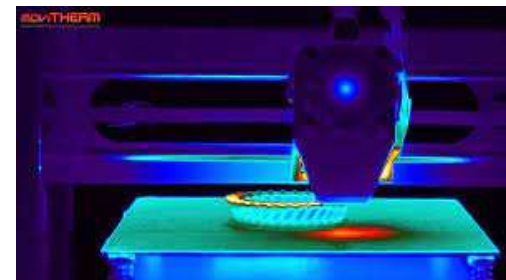


- **Flexible and agile responses:** disruptions, new products, customization
- **Advanced technology needs:** faster, higher-resolution, multi-material, multi-phase dynamics
- **Multiple domain dependencies:** spatial, temporal, material phase



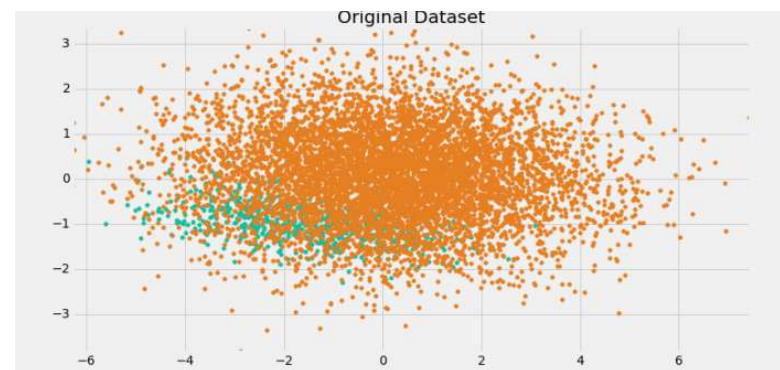
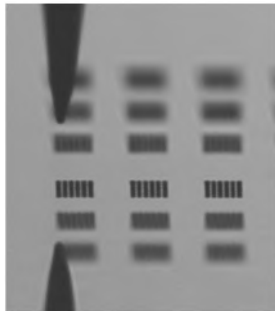
Printed sensor tattoos

[nicoledigiuse.com](http://nicoledigiuse.com)



## Advantages

## Challenges





# Outline

Basic Overview:  
Learning in Manufacturing

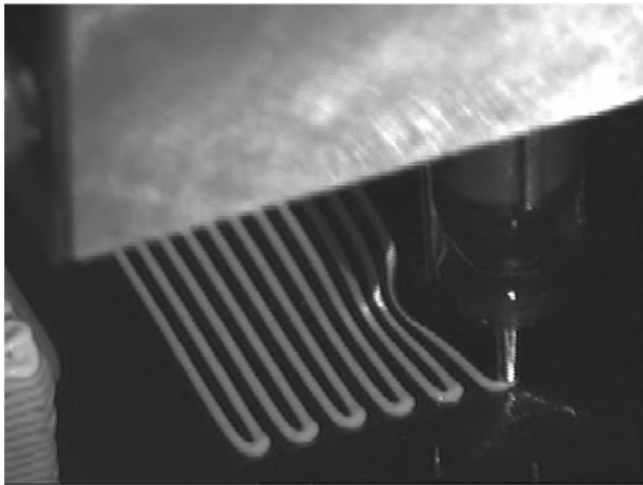
**Learning Case Study:**

- A. Challenges in additive manufacturing modeling and control**
- B. Learning applied to an additive manufacturing example

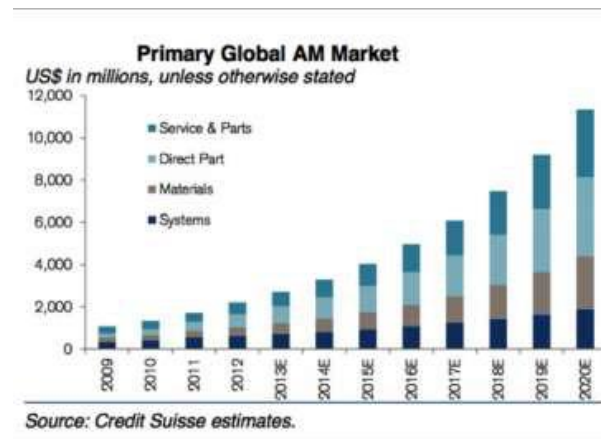
Open Opportunities for Learning + Control to Advance Manufacturing



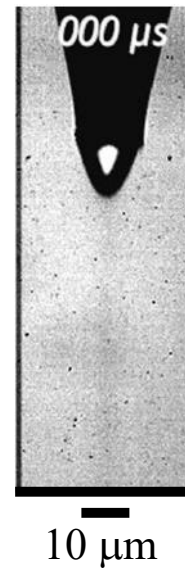
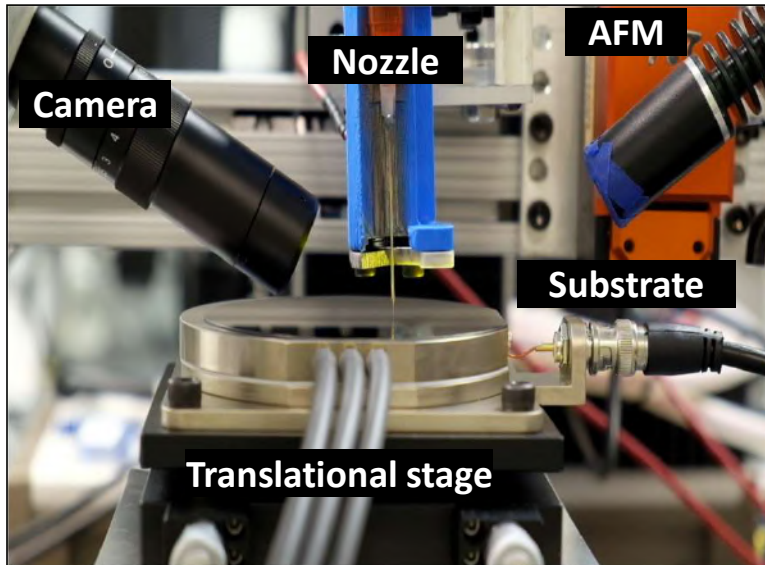
# Additive Manufacturing – diverse application domain



**Extrusion Printing**



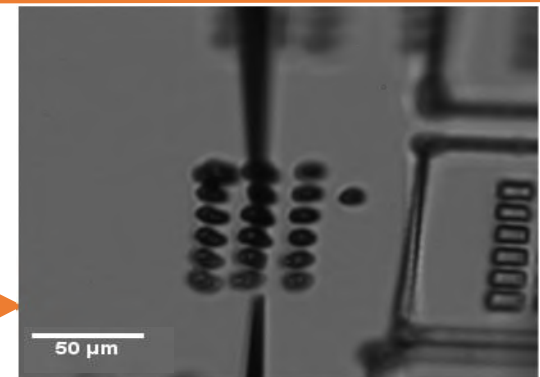
# Introduction – Electrohydrodynamic jet (e-jet) Printing



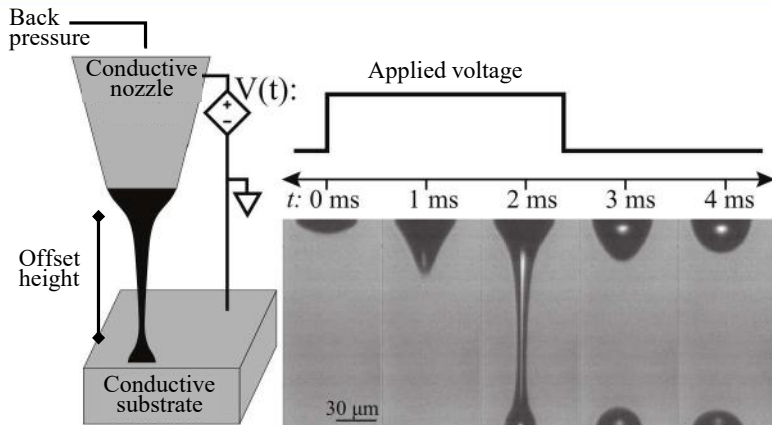
## Advantages:

- Micro-Nano scale resolution
- Multi-material capability
- Non-planar substrates
- Enable complex designs
- Repeatable
- Fast
- Not expensive

How can learning and control lead to enhanced printing performance?



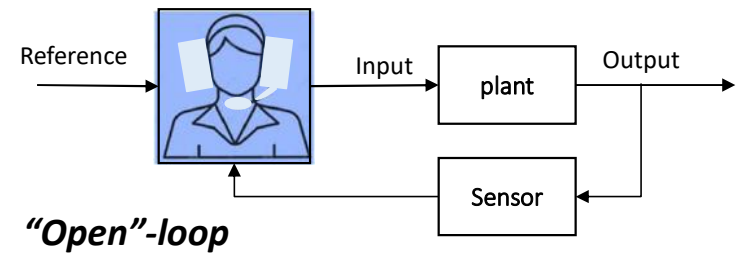
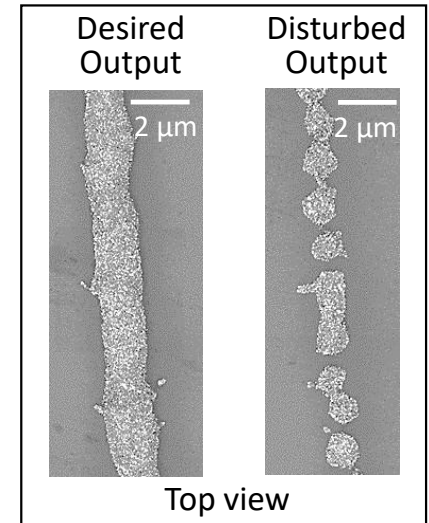
# Challenges in Additive Manufacturing



## Process / Design Parameters:

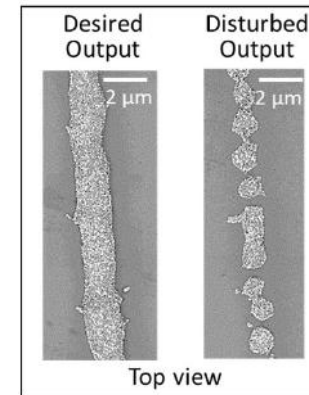
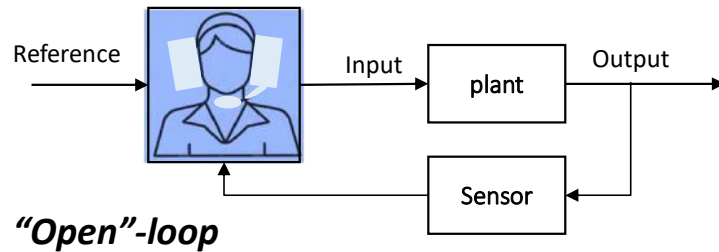
- Ink material / properties
- Substrate material / treatments
- Nozzle material
- Nozzle size / shape
- Offset height between nozzle/substrate
- Back pressure
- Applied voltage signal: DC, pulse - parameters
- Stage speed

## Spraying

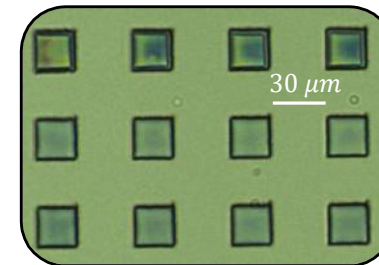
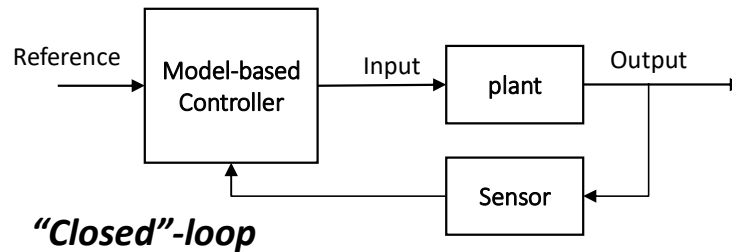
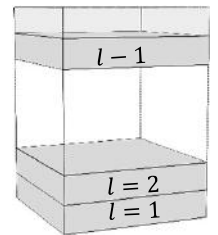


**Manual process parameter tuning limits the speed and adoption of many additive manufacturing processes**

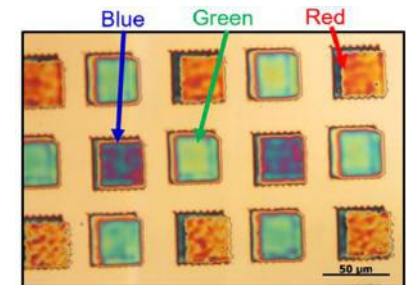
# Challenges in Additive Manufacturing



**Tuned Output**

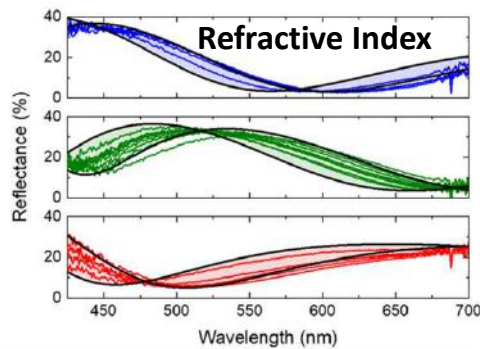
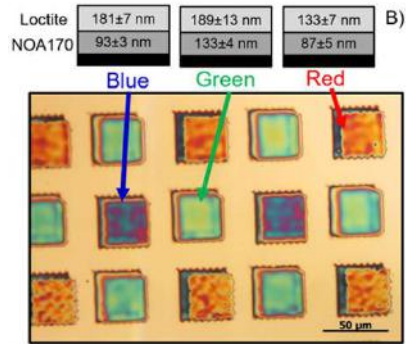
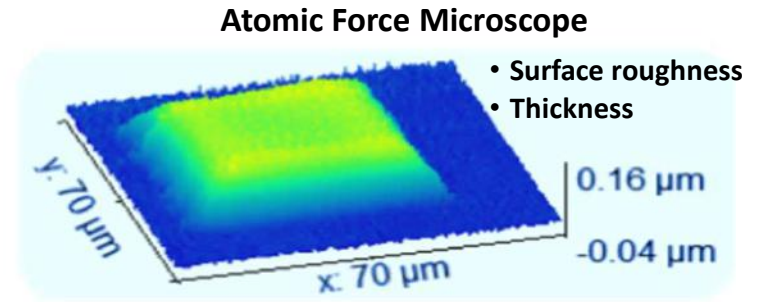
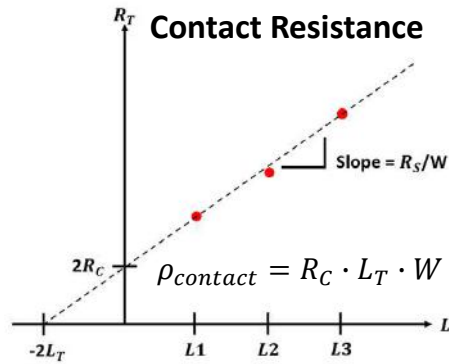
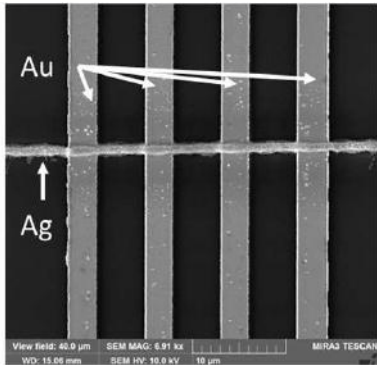


**Controlled Output**

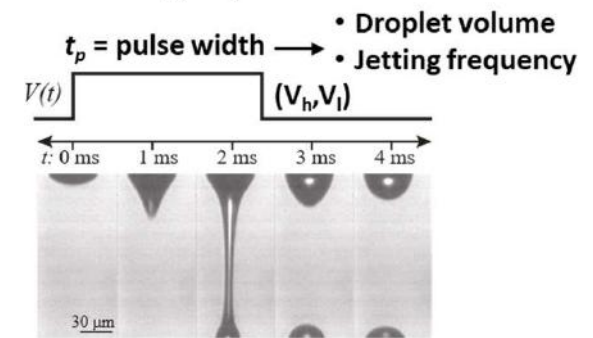


Why is real-time feedback not a viable option for this process?

# Challenges in Additive Manufacturing - Sensing



## High-Speed Camera

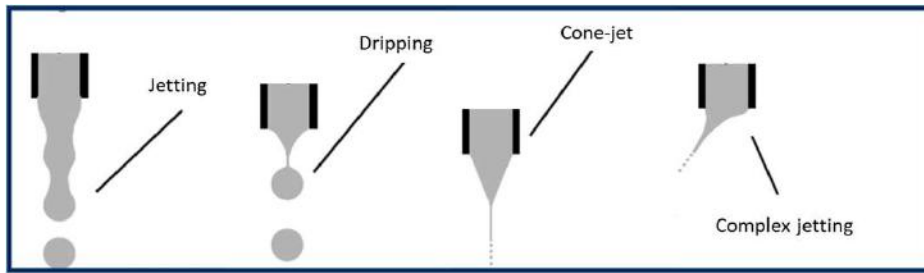


Indirect measurements with inferred behavioral responses

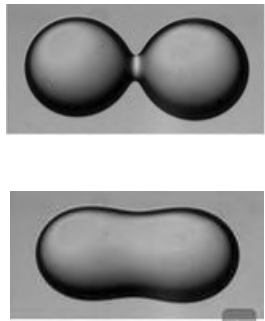
Fast temporal dynamics + high-resolution spatial dynamics

Critical dynamics are too fast or too small, while the true behaviors of interest cannot be monitored in real time

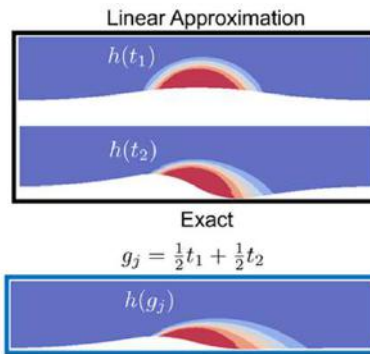
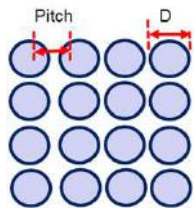
# Challenges in Additive Manufacturing - Modeling



**Jetting Dynamics**



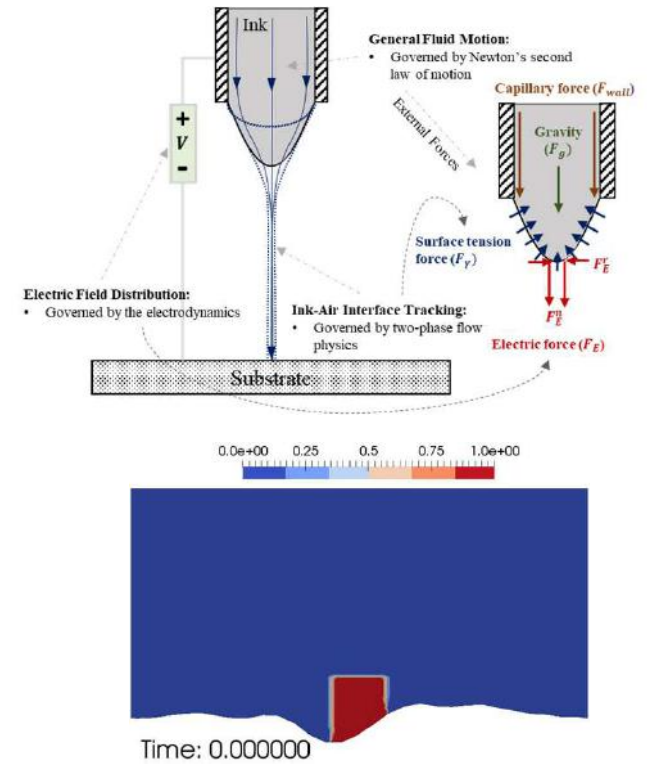
**Droplet merging**



**Droplet impingement**

## Multimodality

Governing physics are complex and often difficult to write as a simple ODE



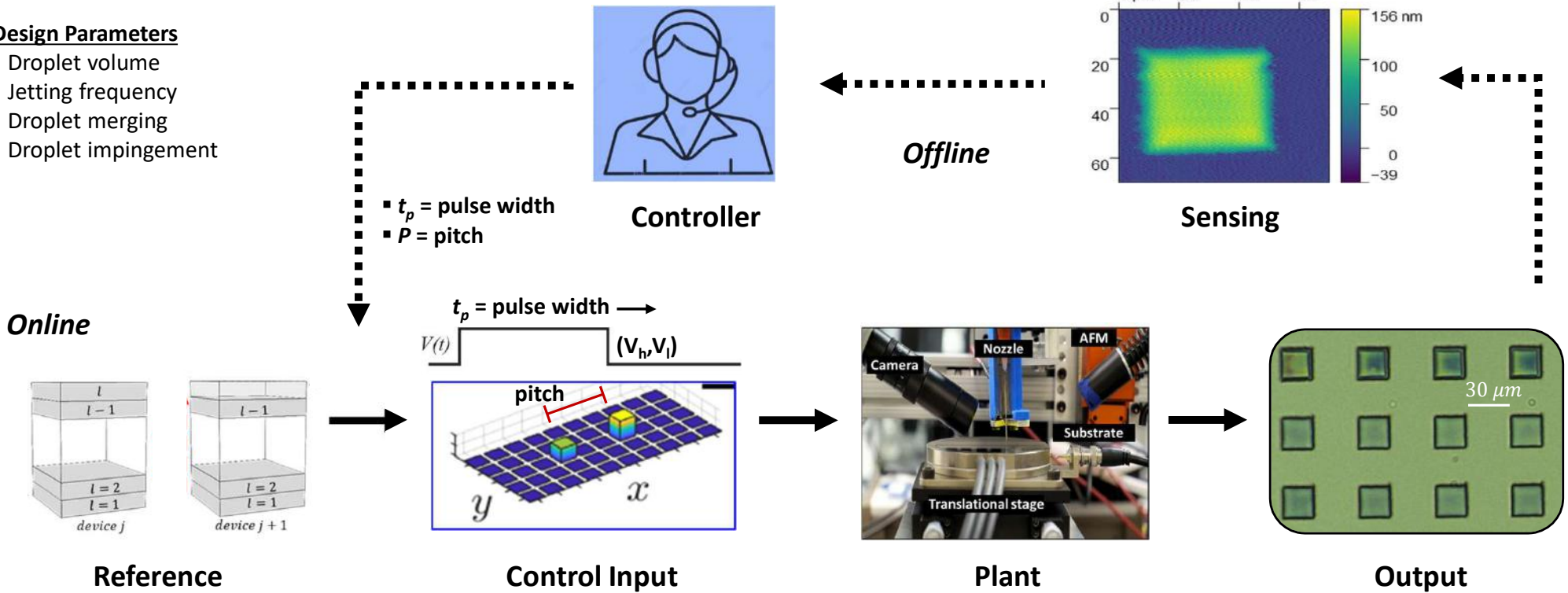
## Multiphysics



# Challenges in Additive Manufacturing - Control

## Design Parameters

- Droplet volume
- Jetting frequency
- Droplet merging
- Droplet impingement



## Control challenges:

- High-speed temporal dynamics
- High-resolution spatial dynamics
- No real-time sensing
- Unmodelled dynamics

**Dynamics are not conducive to real-time feedback control.  
Could leverage repetitive behaviors to control iteratively.**



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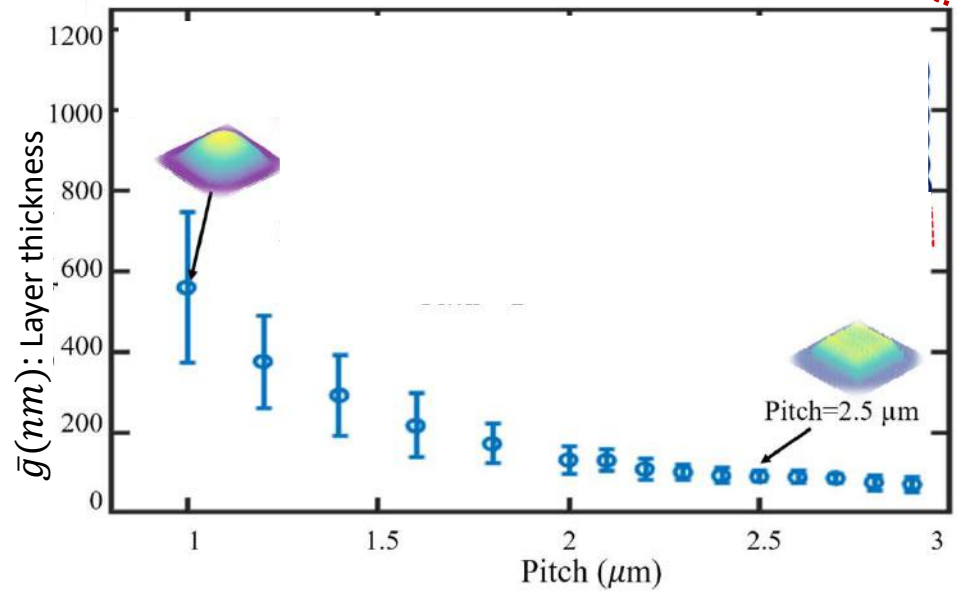
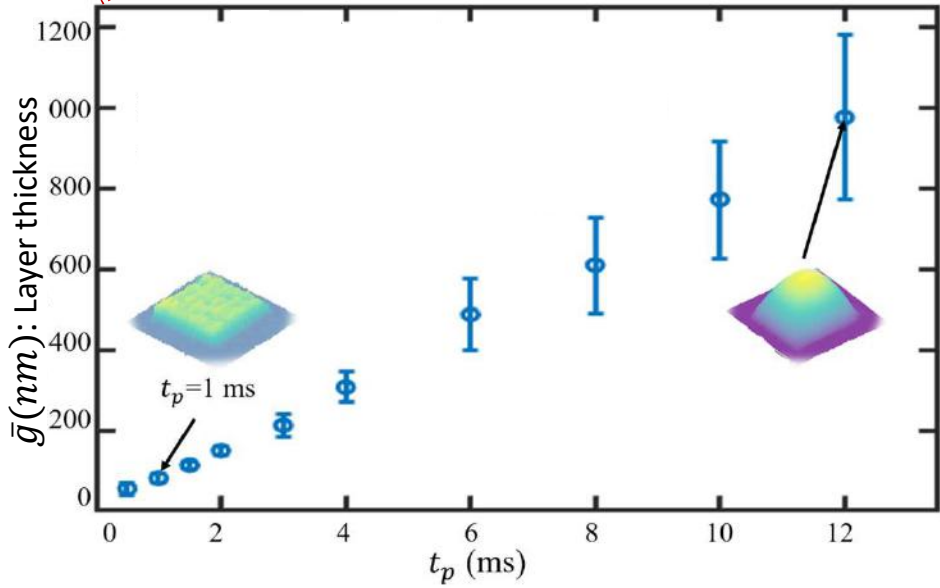
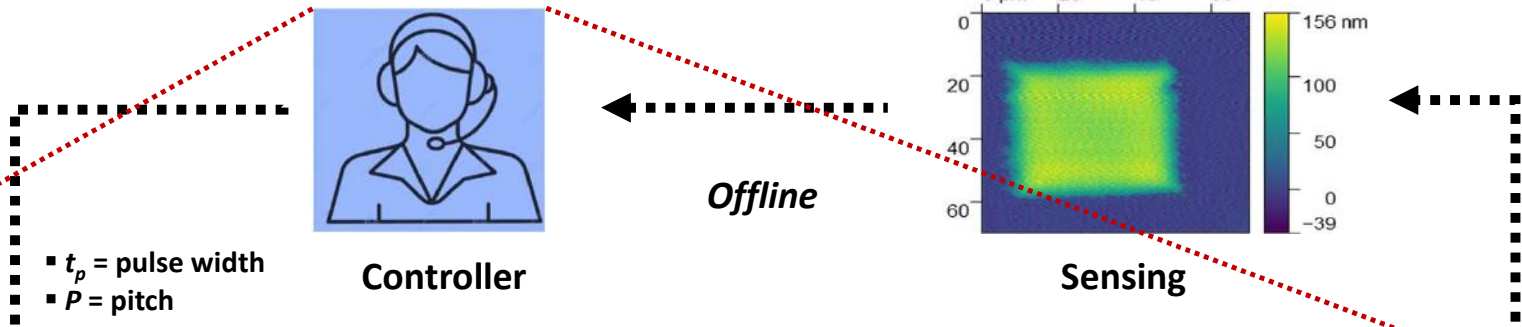
- A. Challenges in additive manufacturing modeling and control
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Open Opportunities for Learning + Control to Advance Manufacturing

# Opportunities to Use Learning in Additive Manufacturing - Control

## Design Parameters

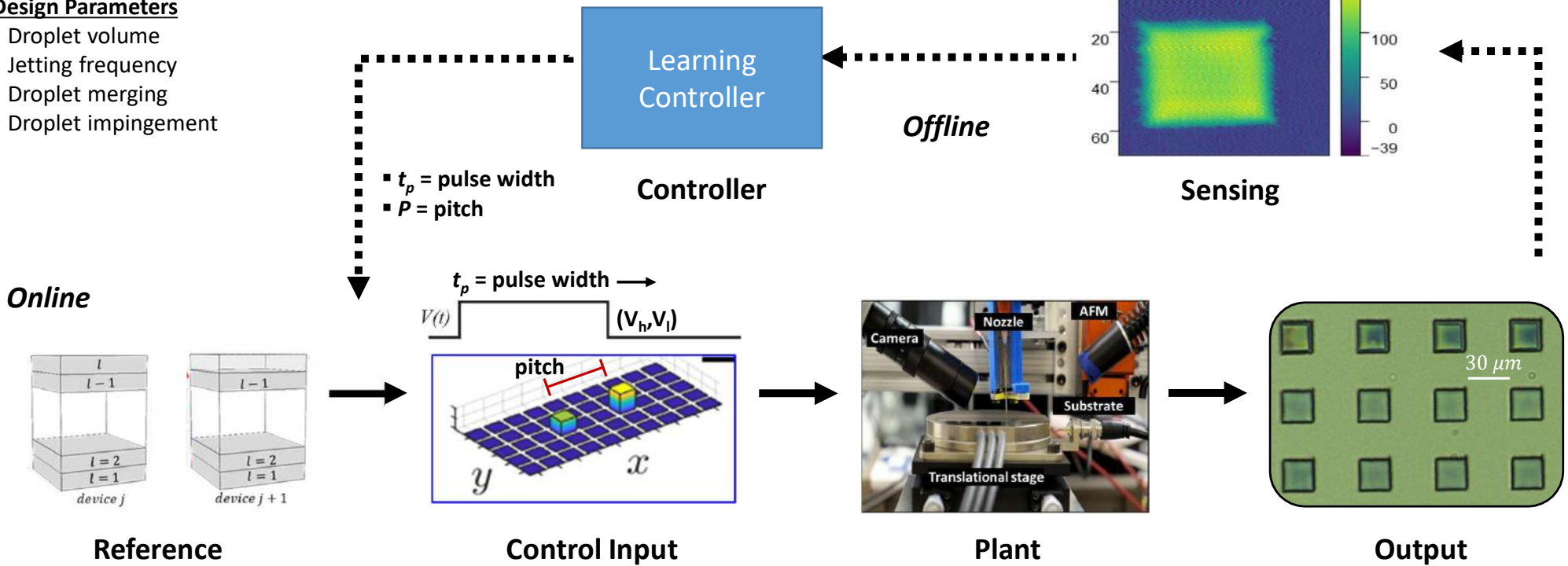
- Droplet volume
- Jetting frequency
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- Droplet impingement



# Opportunities to Use Learning in Additive Manufacturing - Control

## Design Parameters

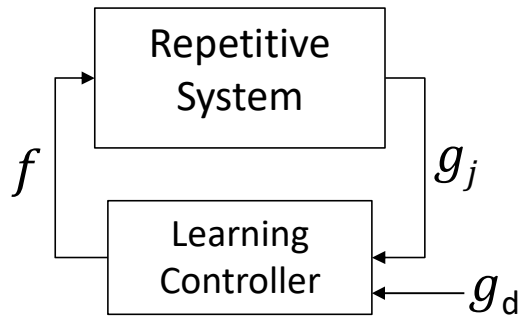
- Droplet volume
- Jetting frequency
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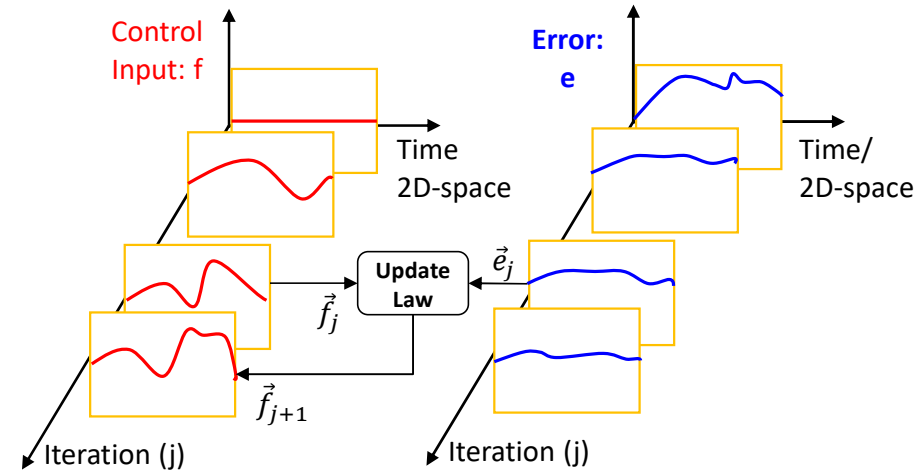
- Goals:**
- Autonomous regulation of product quality
  - Automatic data validation and processing

**Inner loop** – Iterative Learning Control for process regulation

# Introduction to Iterative Learning Control (ILC):



- Repetitive systems
- Reject repetitive disturbance
- Robust to model uncertainty
- Use past input and error signals



- $j$ : Iteration number
- $f_j$ : Input
- $g_j$ : output
- $g_d$ : Reference
- $e_j$ : Error
- $L_f$ : Input filter
- $L_e$ : Error filter

## First order ILC (FO-ILC):

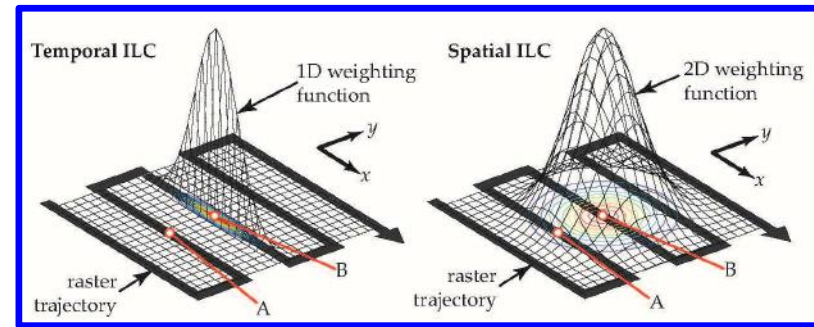
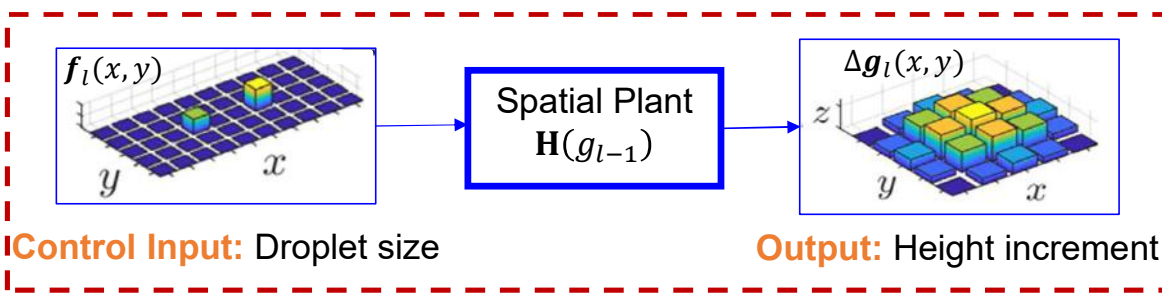
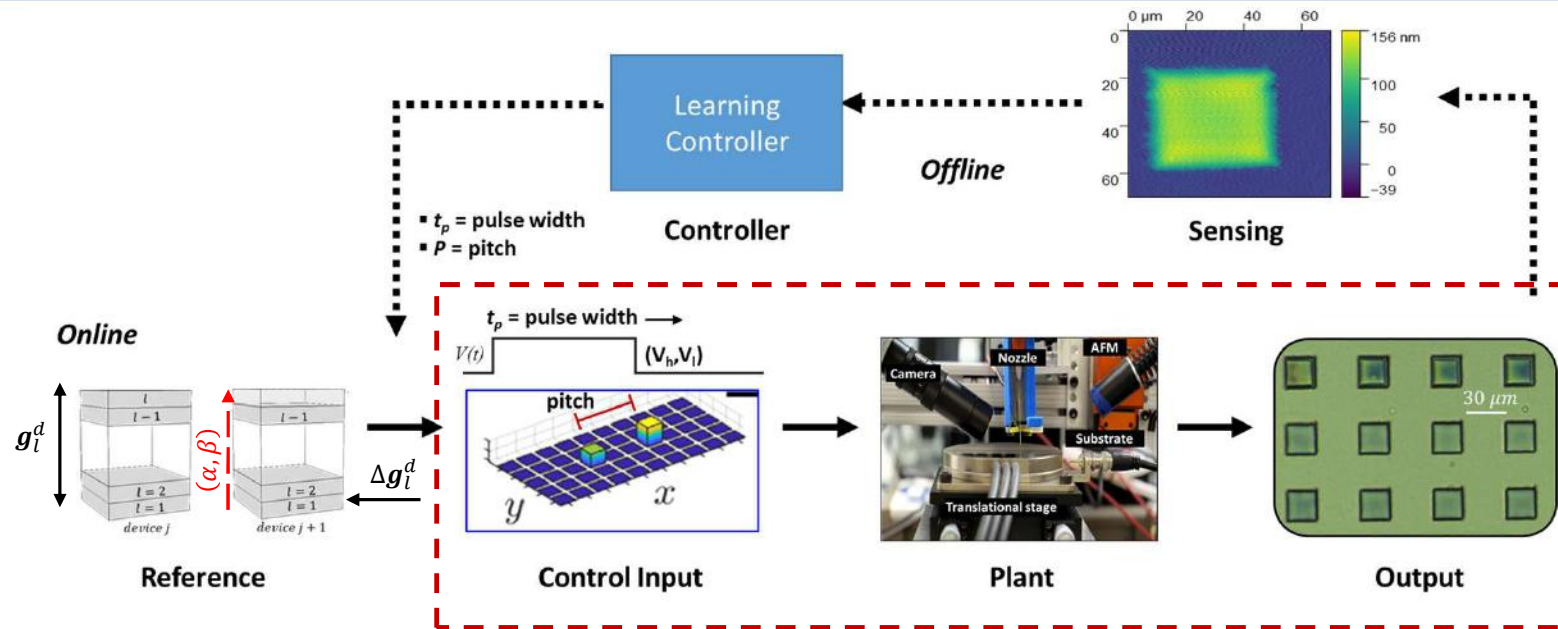
$$\underbrace{f_{j+1}}_{\text{Next iteration input}} = \underbrace{L_f f_j}_{\text{Current iteration input}} + \underbrace{L_e e_j}_{\text{Current iteration error}}$$

$$e_j = g_d - g_j$$

## Higher order ILC (HO-ILC):

$$\vec{f}_{j+1} = \underbrace{\sum_{i=0}^N L_{f_i} f_{j-i} + L_{e_i} e_{j-i}}_{\text{Multiple past iterations}} + \text{Order of ILC}$$

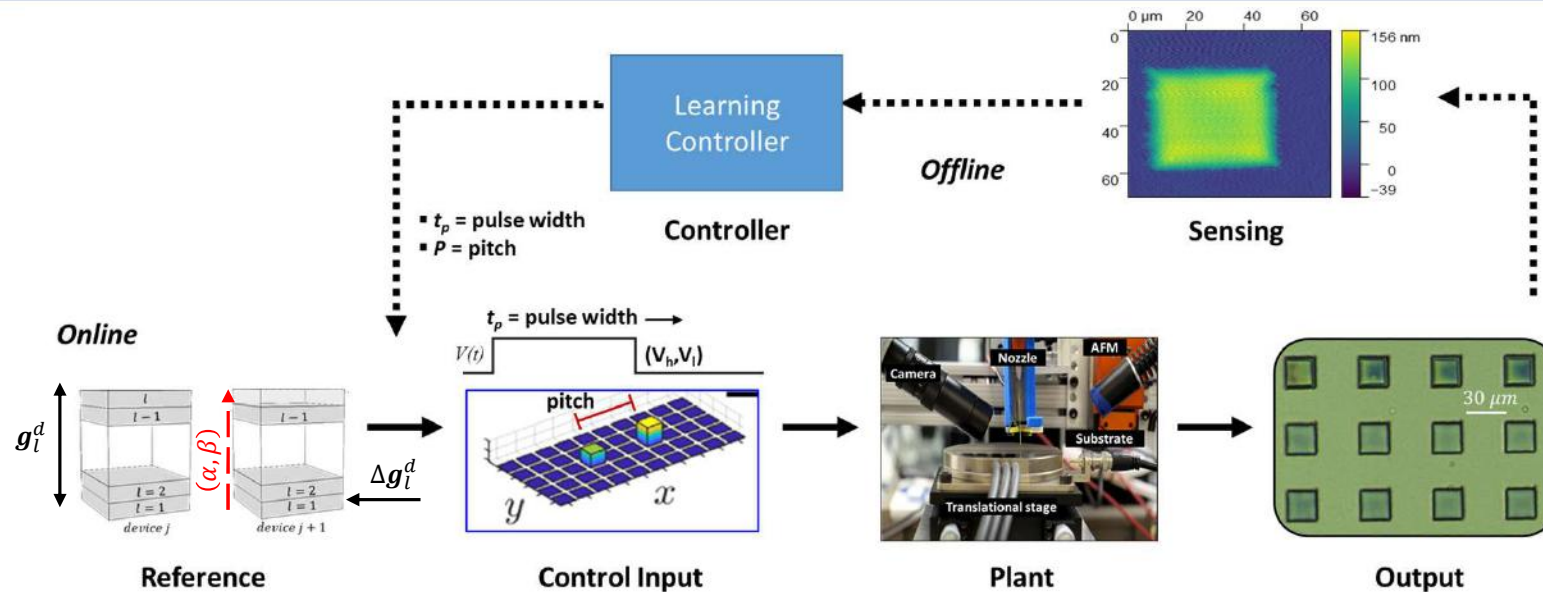
# Spatial Iterative Learning Control (SILC)



**Spatial Plant: 2D Impulse Function**



# Spatial Iterative Learning Control (SILC)

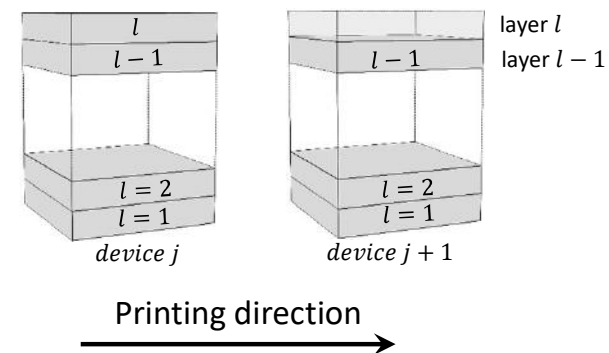


## Performance Objectives:

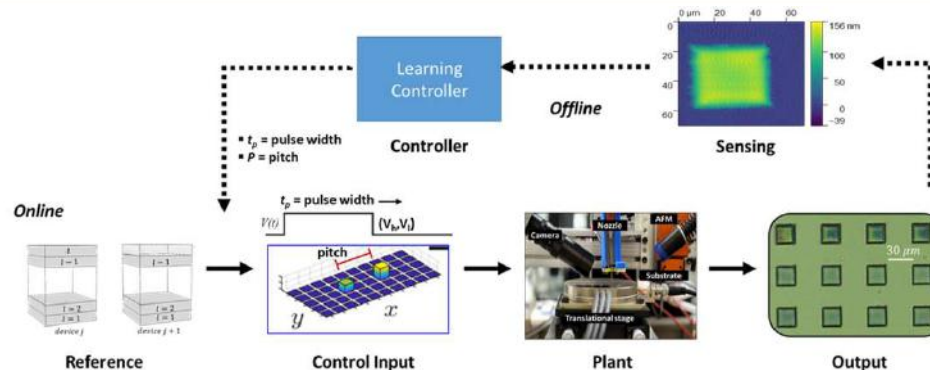
- Total error ( $e_{l,j}$ ) decreases over layers ( $l$ ):  $\vec{e}_{l,j} = g_l^d - \vec{g}_{l,j}$
- Incremental error  $\Delta e_{l,j}$  decreases over layers ( $l$ ) & devices ( $j$ )

$$\Delta \vec{e}_{l,j} \triangleq \Delta \vec{g}_l^d - \Delta \vec{g}_{l,j} = \Delta \vec{e}_l + \alpha_1 \Delta \vec{e}_{l-1} + \dots + \alpha_N \Delta \vec{e}_{l-N}$$

Number of layers:  $\alpha_i = \frac{\alpha}{i} < 1,$



## Controller Design: Norm Optimal SILC Cost Function:



$$\mathfrak{J}_{SILC} = \underbrace{\|\vec{e}_{l,j+1}^w\|_{q.I}^2}_{\text{Performance tracking}} + \underbrace{\|\vec{f}_{l,j+1}\|_{s.I}^2}_{\text{Robustness to model uncertainty}} + \underbrace{\|\vec{f}_{l,j+1} - \vec{f}_{l,j+1}\|_{r.I}^2}_{\text{Convergence rate and noise attenuation over } j} + \sum_{i=1}^{N=L-1} \underbrace{\beta_i \|\vec{f}_{l,j+1} - \vec{f}_{l-i,j+1}\|_{r.I}^2}_{\text{Convergence rate and noise attenuation over } l}$$

$$\Delta \vec{e}_{l,j} \triangleq \Delta \vec{g}_l^d - \Delta \vec{g}_{l,j} = \Delta \vec{e}_l + \alpha_1 \Delta \vec{e}_{l-1} + \dots + \alpha_N \Delta \vec{e}_{l-N}$$

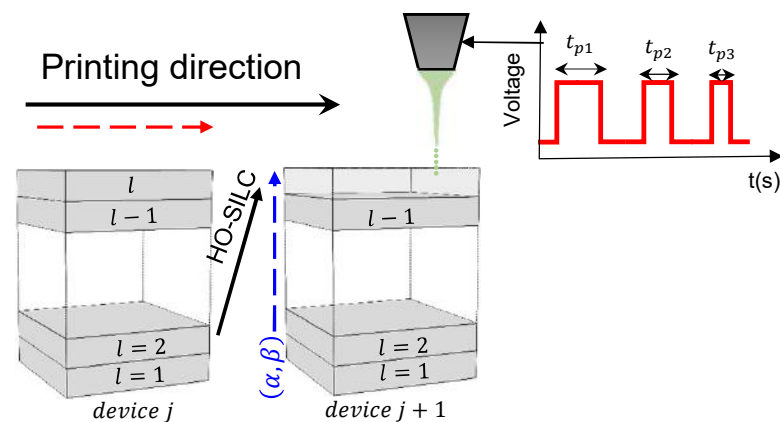
Number of layers:  $\alpha_i = \frac{\alpha}{i} < 1$ ,  $\beta_i = \frac{\beta}{i} < 1$

<p><b>Solve:</b></p> $\frac{\partial \mathfrak{J}_{SILC}}{\partial \vec{f}_{l,j+1}} = 0$	<p><b>Learning Filters:</b></p> $\mathbf{L}_f(q, s, r, \alpha, \beta)$ $\mathbf{L}_e(q, s, r, \alpha, \beta)$
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## Controller Design: SILC Update Law:

$$\vec{f}_{l,j+1} = \underbrace{\mathbf{T}_{l-1,j}^h}_{\text{Horizontal learning}} \vec{f}_{l,j} + \underbrace{\mathbf{T}_{l-2,j}^{v1} \vec{f}_{l-1,j+1} + \dots + \mathbf{T}_{l-N,j}^{vN} \vec{f}_{l-N,j+1}}_{\text{Vertical learning}} + \left( \mathbf{L}_e^h + \sum_{i=1}^{N=L-1} \mathbf{L}_e^{vi} \right) \Delta \vec{g}_l^d$$

$$\begin{cases} \mathbf{T}_{l,j}^h = \mathbf{L}_f^h - \mathbf{L}_e^h \mathbf{H}_{l,j} & \text{Horizontal CL-plant matrix} \\ \mathbf{T}_{l,j}^{vi} = \mathbf{L}_f^{vi} - \mathbf{L}_e^{vi} \mathbf{H}_{l,j} & \text{Vertical CL-plant matrix} \end{cases}$$



## Convert higher order to first order for analysis

$$\vec{Z}_l = \begin{bmatrix} \vec{f}_l \\ \vdots \\ \vec{f}_2 \\ \vec{f}_1 \end{bmatrix}$$

### FO-ILC update law:

$$\vec{Z}_{l,j+1} = \mathbf{F}_{l,j} \vec{Z}_{l,j} + \vec{R}_r \rightarrow \mathbf{F}_{l,j} = \mathcal{F}(\mathbf{T}_{l,j}^h, \mathbf{T}_{l,j}^{vi})$$

**F is high dimensional**

## Controller Design: Stability Analysis:

**FO-ILC update law:**  $\vec{Z}_{l,j+1} = \mathbf{F}_{l,j} \vec{Z}_{l,j} + \vec{R}_r$        $\mathbf{F}_{l,j} = \mathcal{F}(\mathbf{T}_{l,j}^h, \mathbf{T}_{l,j}^{vi})$

**Goal: Asymptotic stability:**  $\rho(\mathbf{F}_0) < 1$

- Estimate the robustness radius ( $\|\Delta\mathbf{H}_{l,j}\| < r_{AIU}$ ) such that the iteration varying SILC update law remains stable ( $\|\mathbf{F}_{l,j}\| < 1$ )
- How do we design  $r_{AIU}$  to ensure robustness?

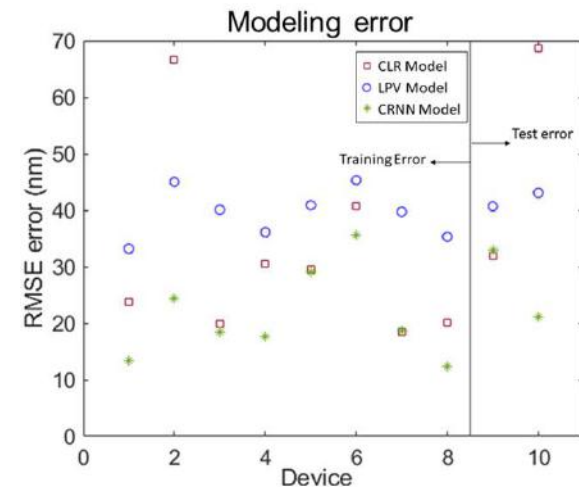
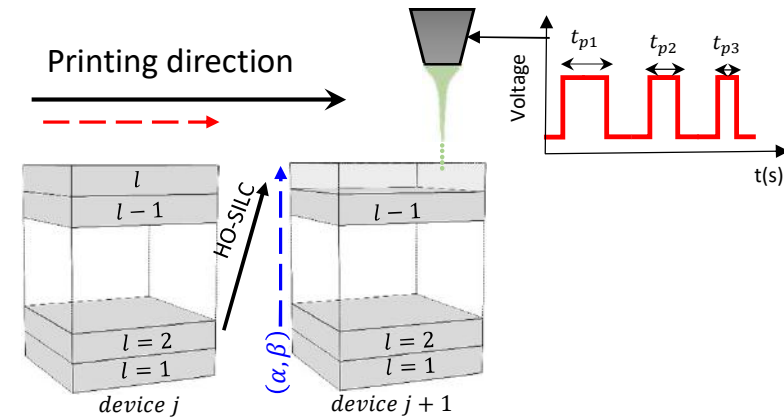
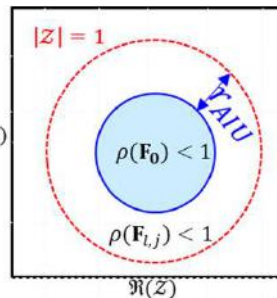
$$\mathbf{H}_{l,j} = \underbrace{\mathbf{H}_0}_{\text{Nominal plant}} + \underbrace{\Delta\mathbf{H}_{l,j}}_{\text{Model uncertainty}}$$

$$\mathbf{F}_{l,j} = \underbrace{\mathbf{F}_0}_{\text{Nominal}} + \Delta\mathbf{F}_{l,j}(\Delta\mathbf{H}_{l,j})$$

$$\|\Delta\mathbf{H}_{l,j}\| < \boxed{r_{AIU}} \text{ design}$$

**Robustness radius design:**  $r_{AIU}(q, s, r, \alpha, \beta)$

SILC
HO-SILC

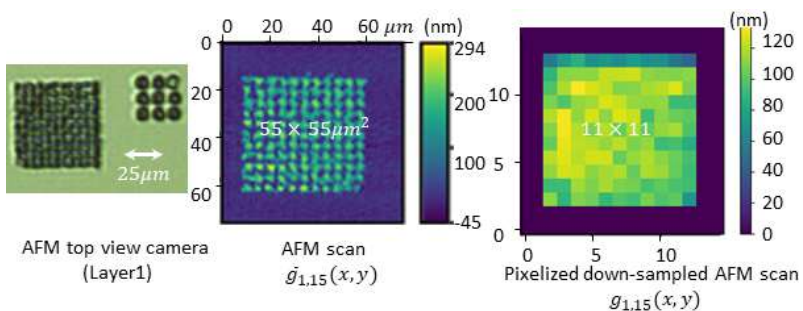


Z Afkhami, et al. TCST, (2022).  
Afkhami, Hoelzle, Barton, (2022). IFAC-PapersOnLine  
Pannier et al. 2019  
E. Balta, et al. TCST 2021.

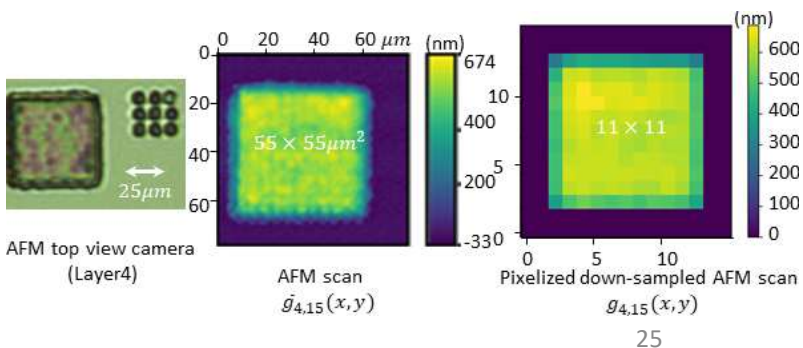
## Controller Performance:

### HO-SILC Experimental Results

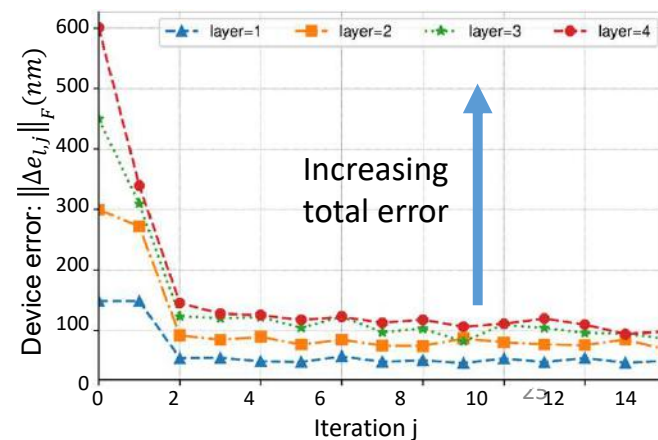
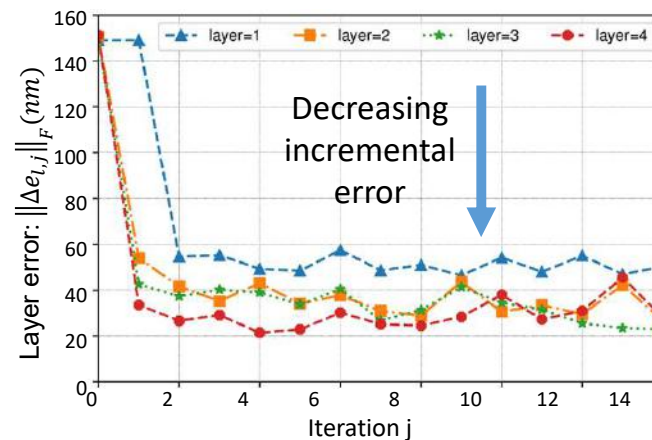
Layer=1



Layer=4

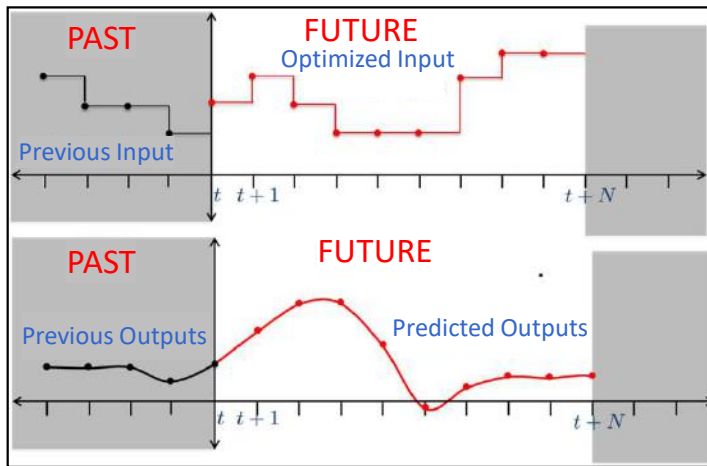


### HO-SILC Errors

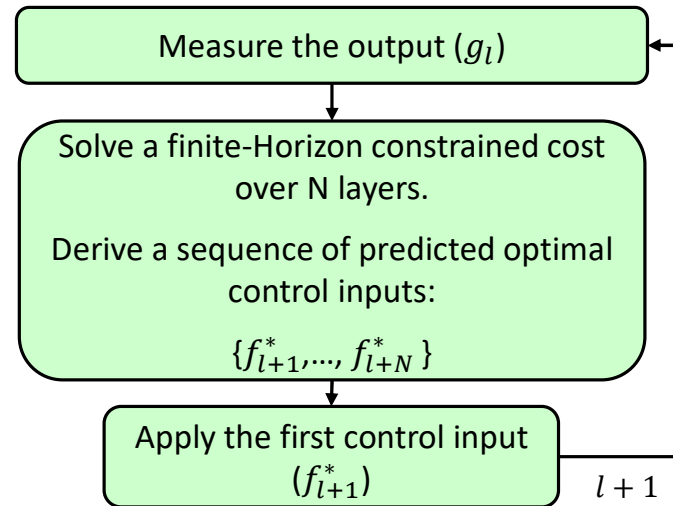


Can we do anything to address the increasing errors?

# Model Predictive Control (MPC)



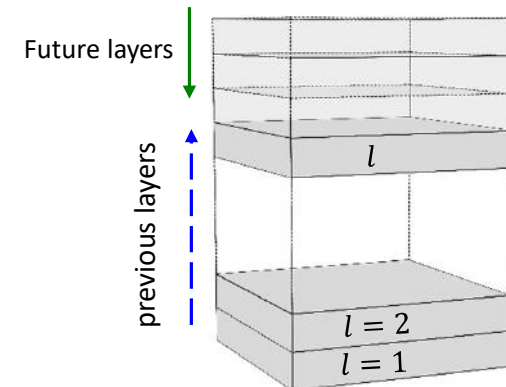
Modified figure from EECE119-M22 course by S. Di Cairano and I. Kolmanovsky



Leverage MPC to enhance robustness

## Goal:

- Learn from previous layers using SILC design
- Predict future layer deposition errors using MPC design
- Predict the optimal input signal of multiple layers ahead ( $\vec{f}_{l+1}^*, \dots, \vec{f}_{l+N}^*$ )
- At each printing pass, only the input signal of the first layer,  $\vec{f}_{l+1}^*$ , is considered



Z Afkhami, et al. TCST, (2022).  
Afkhami, Hoelzle, Barton, (2022). IFAC-PapersOnLine



**SILC cost function:**

$$\mathfrak{J}_{SILC} = \underbrace{\|\vec{e}_{l+1}\|_{Q_{e1}}^2}_{\text{Performance tracking}} + \underbrace{\|\Delta\vec{e}_{l+1}\|_{Q_{\Delta e}}^2}_{\text{Robustness to model uncertainty}} + \underbrace{\|\vec{f}_{l+1}\|_{S_1}^2}_{\text{Convergence rate and noise attenuation}} + \underbrace{\|(\vec{f}_{l+1} - \vec{f}_l)\|_{R_1}^2}_{\text{Convergence rate and noise attenuation}}$$

**MPC cost function:**

$$\mathfrak{J}_{MPC} = \underbrace{P_N \|\vec{e}_{l+N}\|_I^2}_{\text{Terminal cost}} + \underbrace{\sum_{i=2}^N \|\vec{e}_{l+i}\|_{Q_{e_i}}^2 + \|\vec{f}_{l+i}\|_{S_i}^2 + \|(\vec{f}_{l+i+1} - \vec{f}_{l+i})\|_{R_i}^2}_{\text{Model predictive horizon}} \quad s.t. \vec{0} < \vec{f}_{l+i} < \vec{F}$$

Improves stability properties

**SILC-MPC cost function:**

$$\mathfrak{J}_{SILC-MPC} = \mathfrak{J}_{SILC} + \mathfrak{J}_{MPC}$$

s.t.  $\vec{0} < \vec{f} < \vec{F}_{\max}$  Bounded control signal

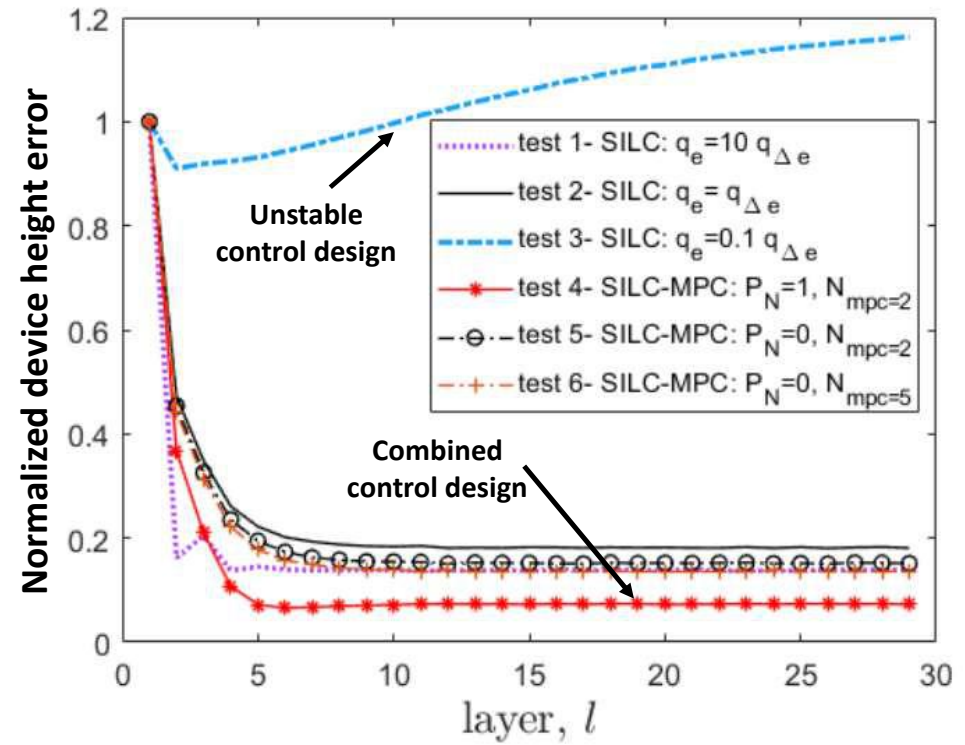
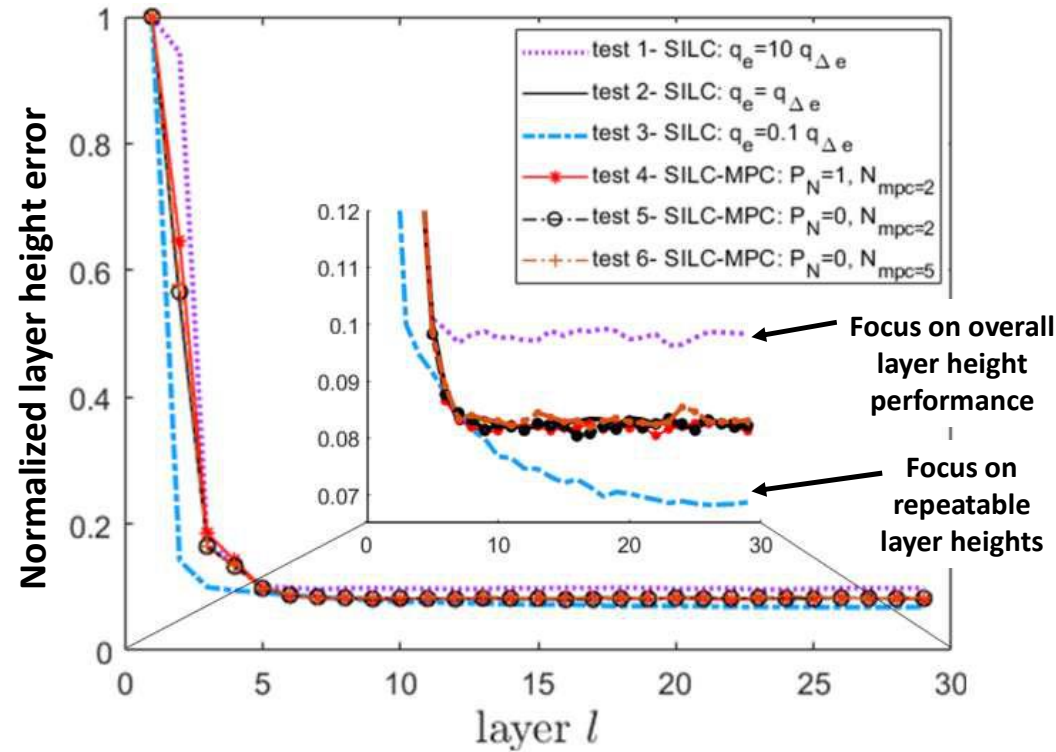
$$S = \begin{bmatrix} S_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & S_N \end{bmatrix}$$

$$R = \begin{bmatrix} R_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & R_N \end{bmatrix}$$

$$Q = \begin{bmatrix} Q_{\Delta e} & & & 0 \\ & Q_{e1} & & \\ & & \ddots & \\ 0 & & & Q_{eN} + P_N I \end{bmatrix}$$

Design matrices

# Simulation Results



Forward prediction and iterative learning control leads to optimal performance



# Outline

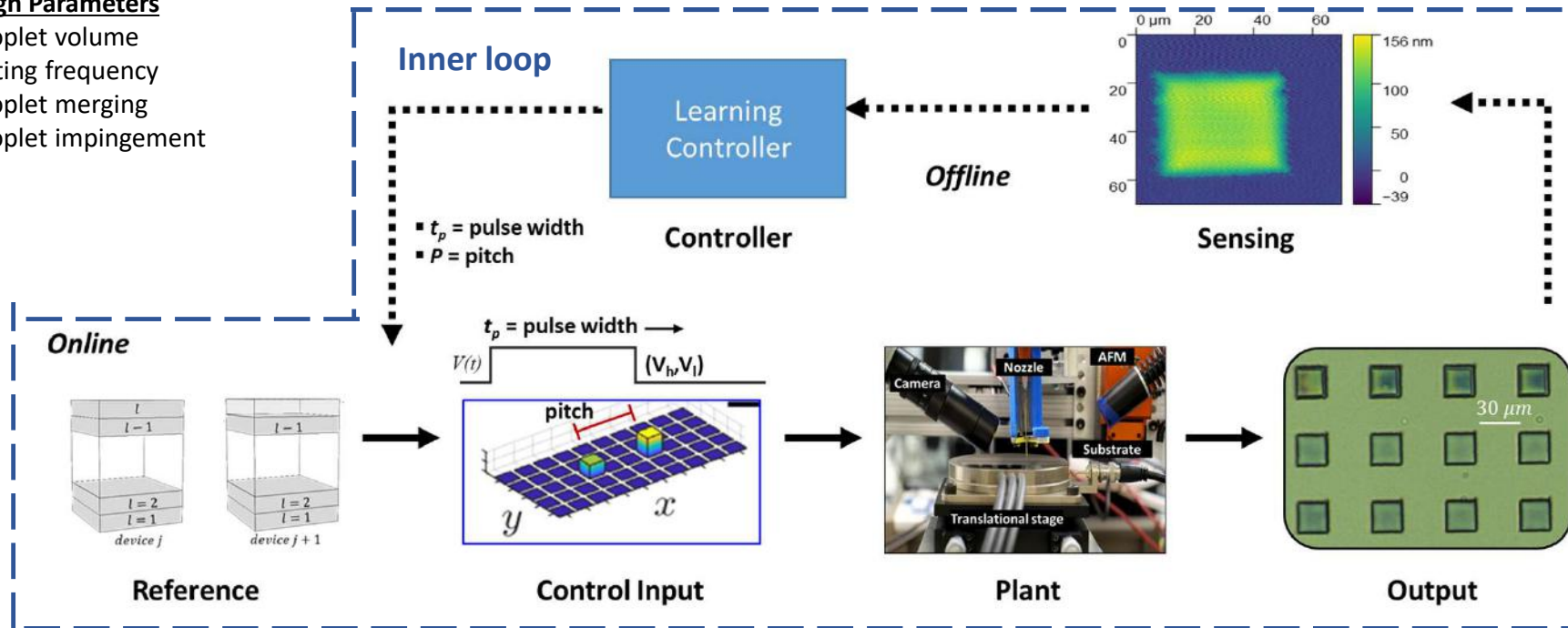
Basic Overview:  
Learning in Manufacturing

Learning Case Study:  
A. Challenges in additive manufacturing modeling and control  
B. Learning applied to an additive manufacturing example

**Open Opportunities for Learning + Control to Advance Manufacturing**

## Design Parameters

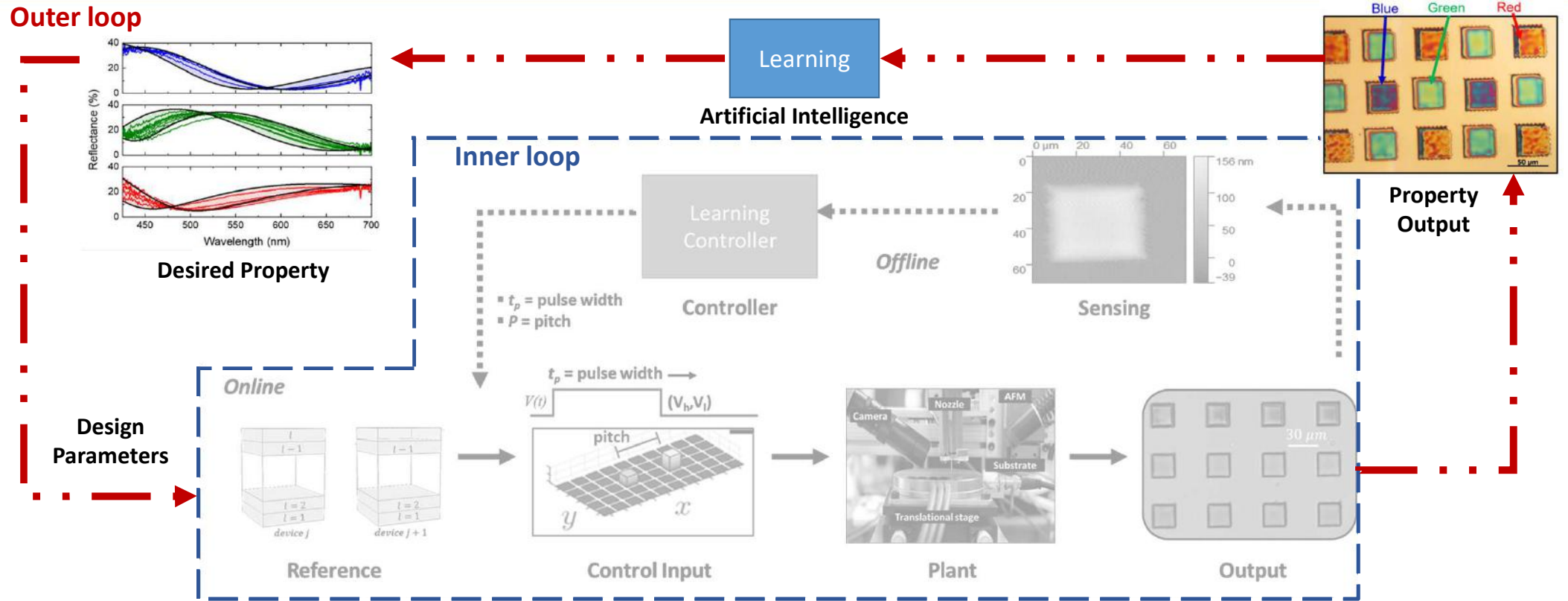
- Droplet volume
- Jetting frequency
- Droplet merging
- Droplet impingement



- Goals:**
- Autonomous regulation of product quality
  - Automatic data validation and processing

**Inner loop** – Iterative Learning Control for process regulation

# Opportunities to Use Learning in Additive Manufacturing - AI



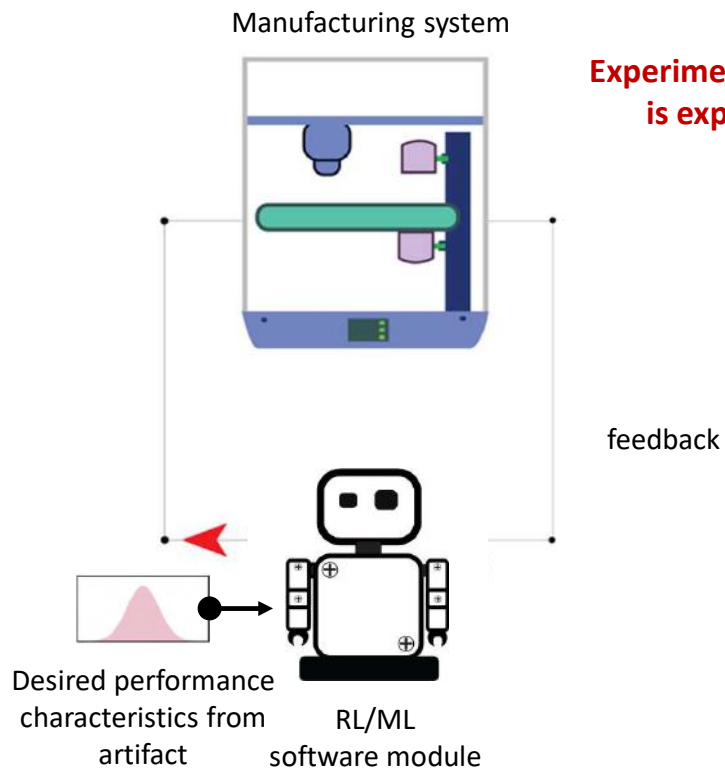
**Goals:** • Automatic identification of process-structure-property relationships

**Outer loop** – Reinforcement Learning for process-structure-property relationships



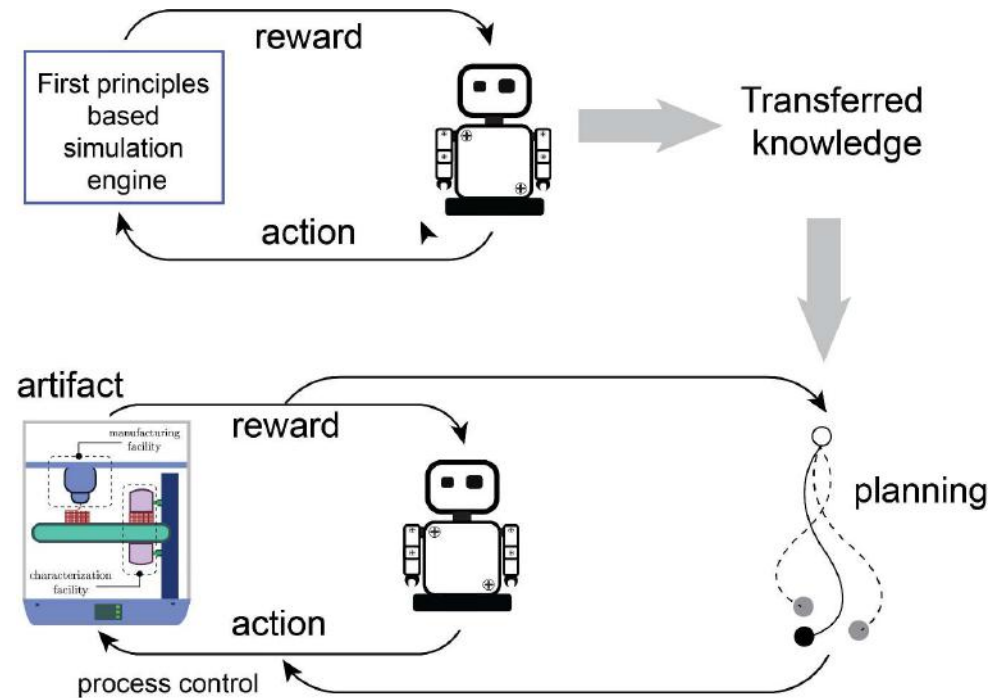
Collaboration with Prof. David Hoelzle's group at Ohio State University

# Opportunities to Use Learning in Additive Manufacturing - AI



**Reinforcement Learning**

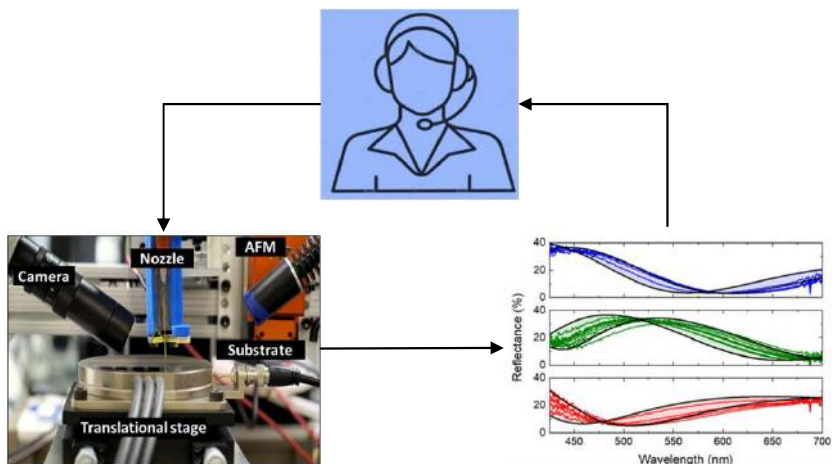
**Experimental testing is expensive!**



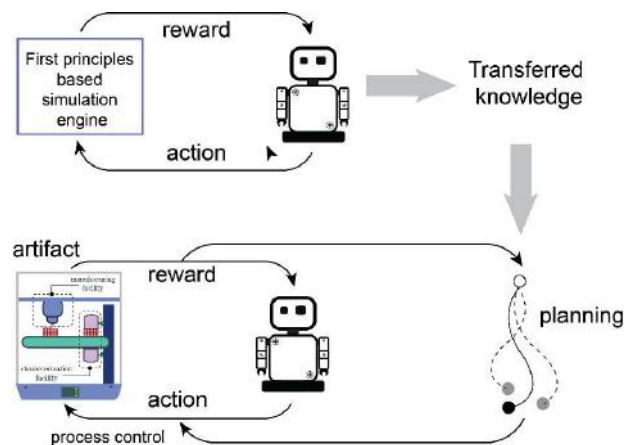
**Transfer learning framework in the context of RL for manufacturing decision making**



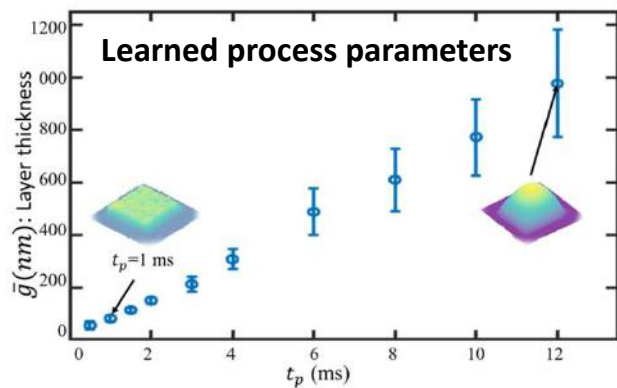
# Reinforcement Learning for Process-Structure-Property Relationship



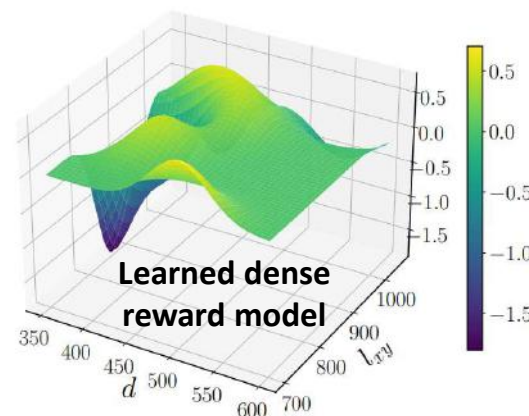
**Brute force learning – [Months]**



**Automated learning – [Hours]**



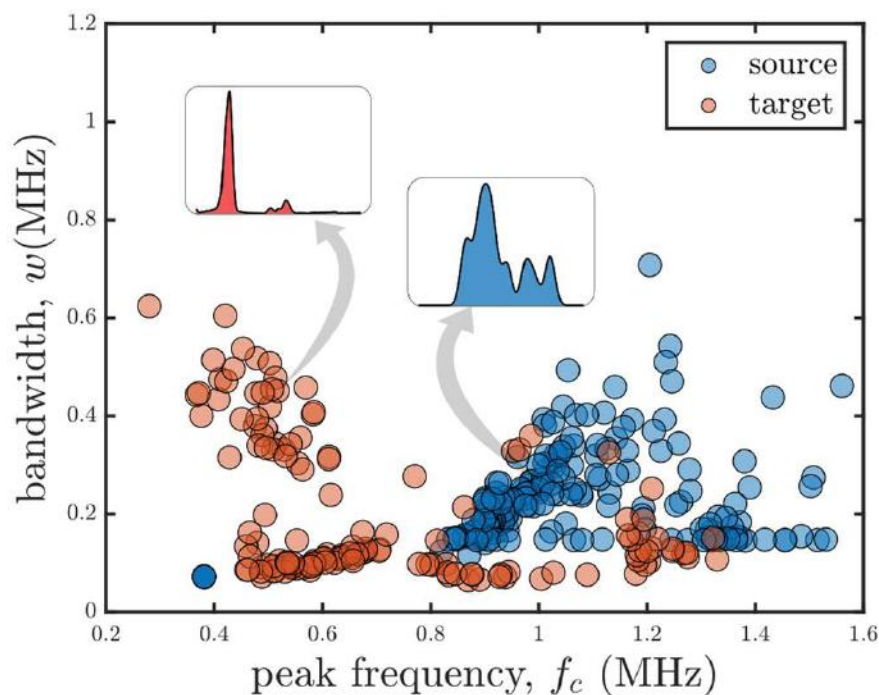
**Human derived process-structure-property relationship**



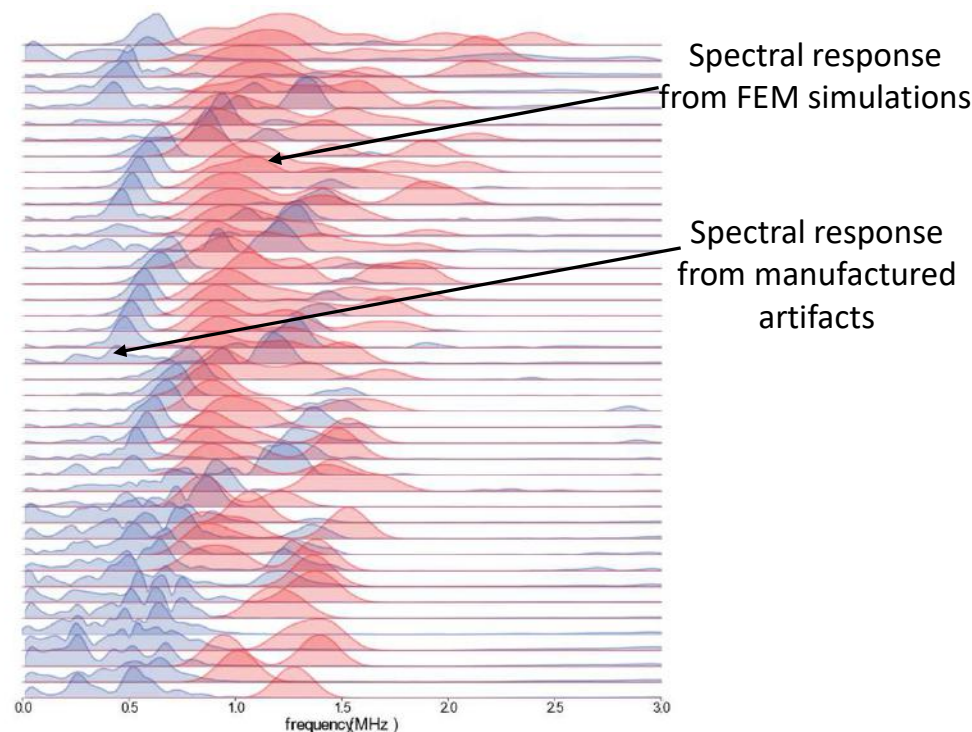
**RL derived process-structure-property relationship**

# Why is implementing Machine learning a challenge in manufacturing systems

Distribution of features changes from simulation model to manufactured artifact

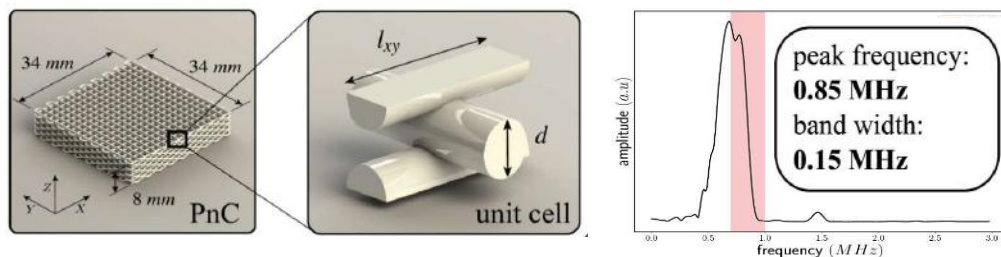
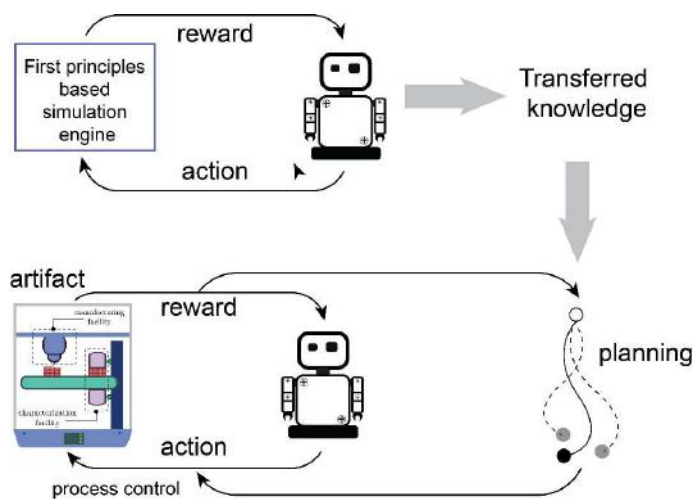


Output characteristics of an artifact change from simulation to manufactured artifact

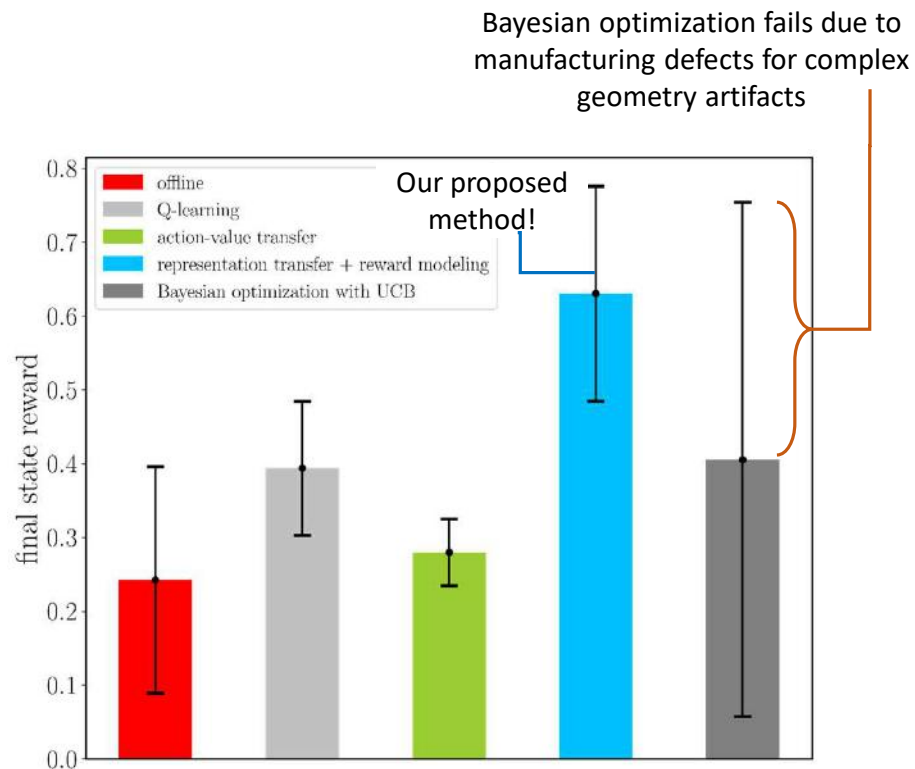


**Need a learning strategy that can handle model uncertainty**

# How do other transfer learning strategies perform?

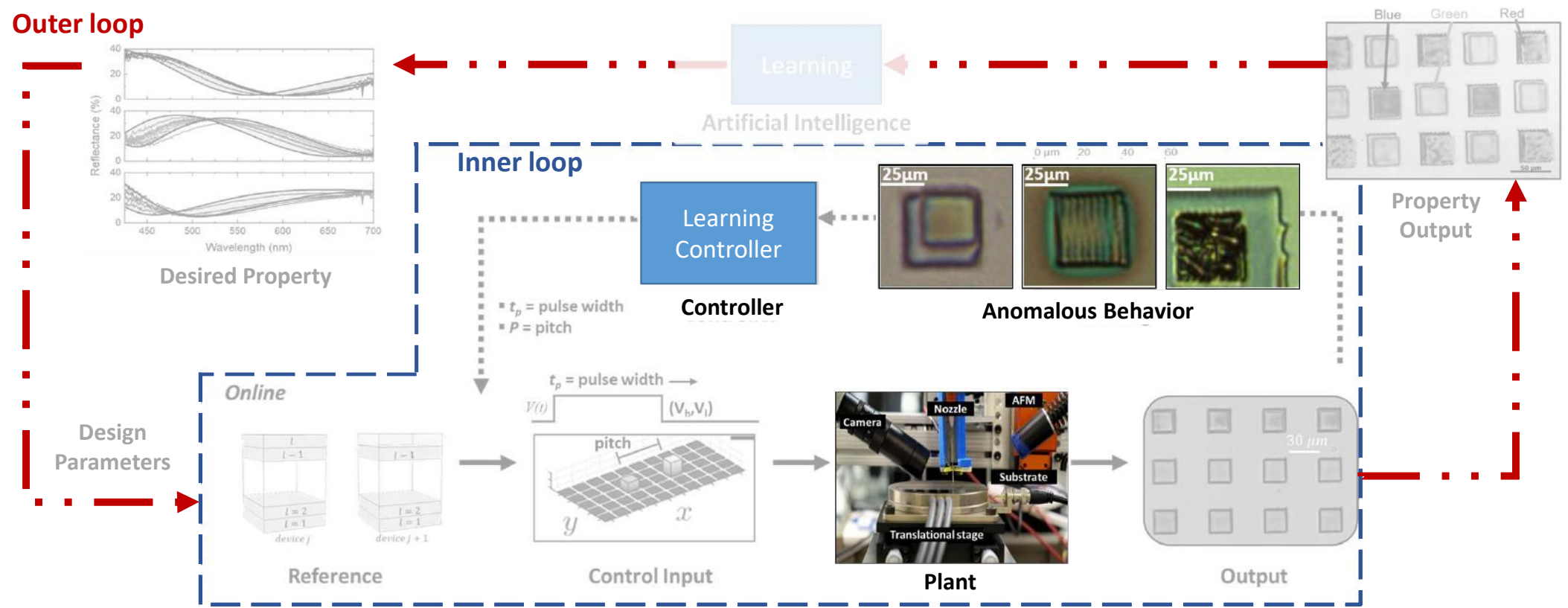


Representation transfer with probabilistic reward modeling



Reward obtained from final artifact

# Opportunities to Use Learning in Additive Manufacturing - AI



## Applications of Learning:

- Control design
- Functional device design
- Model identification and updating
- Anomaly detection and classification
- In situ quality control



## Open Control Questions:

- Performance and robustness guarantees for combined ML + Learning Control mtds.
- Robustness requirements for automatic model updating
- Uncertainties associated with manufacturing defects

Thank you for your  
attention!



# CCTA 2023



- Bridgetown, Barbados
- Venue: Hilton Barbados
- Date: 16-18 August, 2023
- Papers due: Jan. 31, 2023
- <https://ieeeccta.org/>



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- Applied Dynamics International
- Boeing

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- Ohio State University
- University of Illinois
- Air Force Research Lab
- Army Research Lab

**NIST**

**ADI** APPLIED DYNAMICS  
INTERNATIONAL

**Rockwell  
Automation**



**HITACHI**

All the students that have  
contributed to this research!

## For More Information Contact

**Kira Barton**

Associate Professor  
Department of Robotics  
Department of Mechanical Eng.  
[bartonkl@umich.edu](mailto:bartonkl@umich.edu)

# Thank You!